

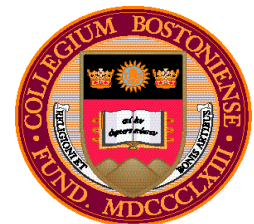
Wave-Optics Analysis of HF Propagation through Traveling Ionospheric Disturbances and Developing Plasma Bubbles

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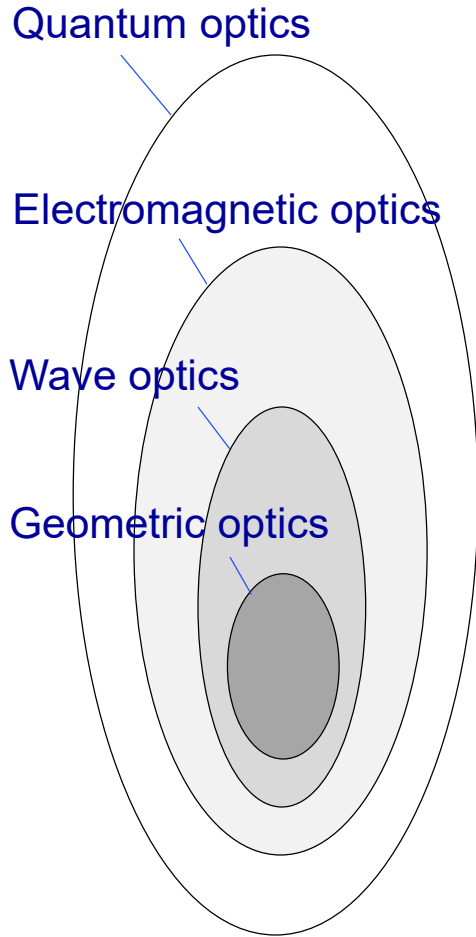
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- We apply a wave-optics technique to model the propagation of high-frequency (HF) waves through simulated traveling ionospheric disturbances (TIDs) and developing plasma bubbles at low latitudes.
- Wave-optics is derived from a forward-propagation approximation of the Helmholtz equation governing the electric field in the frequency domain.
- It is implemented using the split-step approach commonly referred to as the multiple phase screen method (MPS).
- We use the angular spectrum (a byproduct of the computation) to generate angle-of-arrival “maps,” which depict the spectrum of angle-of-arrival (AOA) everywhere on the ground.
- These AOA maps identify all radio propagation modes and their amplitudes. There is no need to ‘home’ rays to identify these propagation modes.
- Wave-optics can represent the interaction (via diffraction) between different propagation modes, which result in fading of the received HF signal. Ray-tracing techniques, by comparison, neglect these effects.

Hierarchy of Wave Propagation Theories



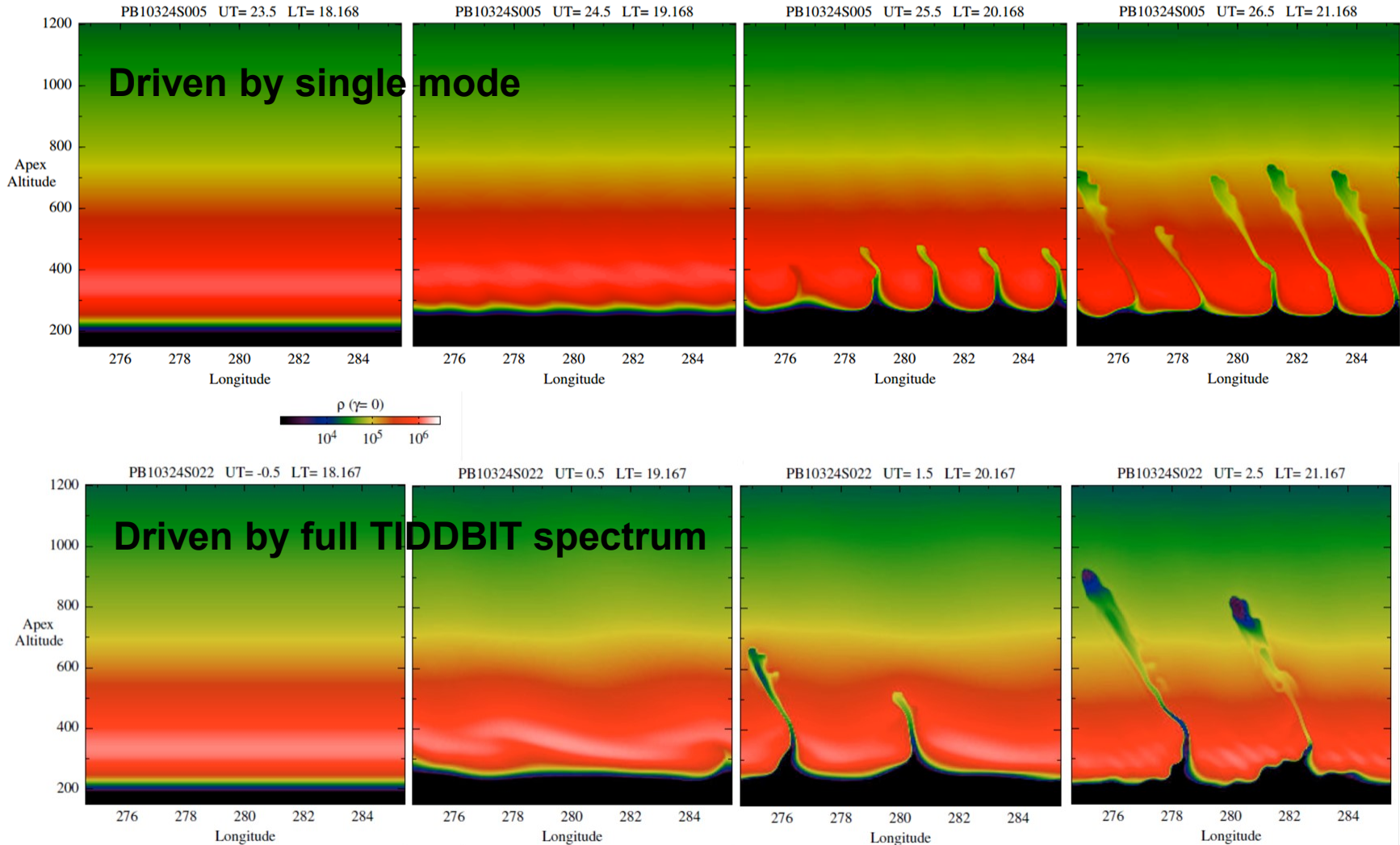
Wave Theory	Simplifying Assumption	Numerical Algorithms
Quantum optics	None(?)	
Electromagnetic optics (Maxwell)	Classical fields	Finite-difference time domain (FDTD)
Wave optics	Scalar waves	Forward propagation equation (FPE)
	Small-angle scatter	Parabolic wave equation (PWE)
		Multiple phase screen (MPS)
Geometric optics	Infinitesimally small λ , no diffraction or interference	Hamiltonian Ray-tracing
	Rays are lines	Snell's Law



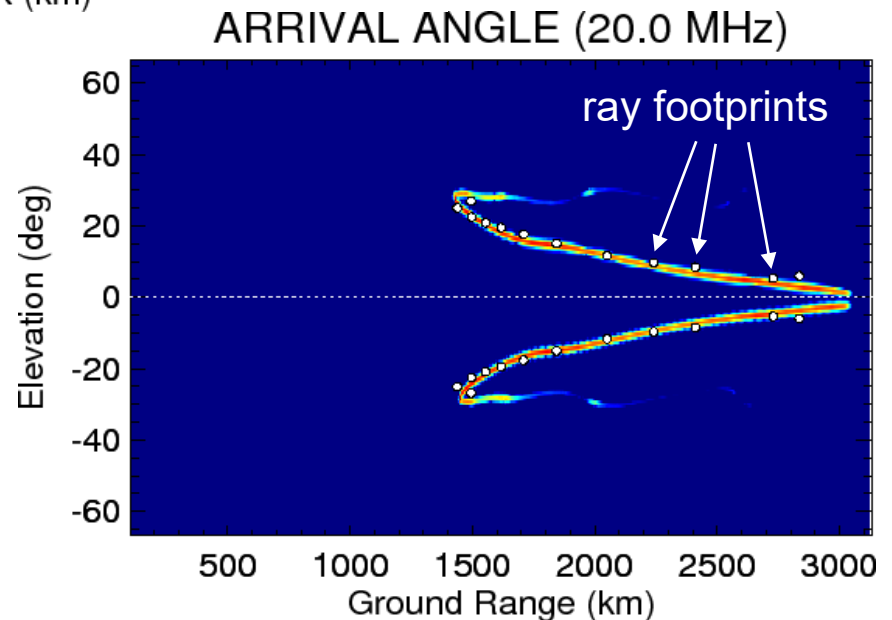
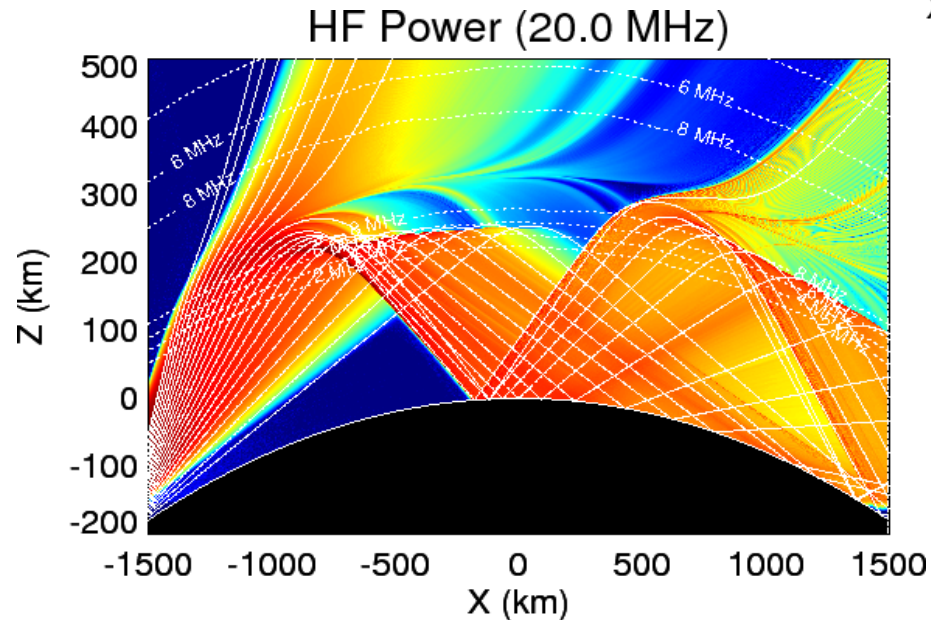
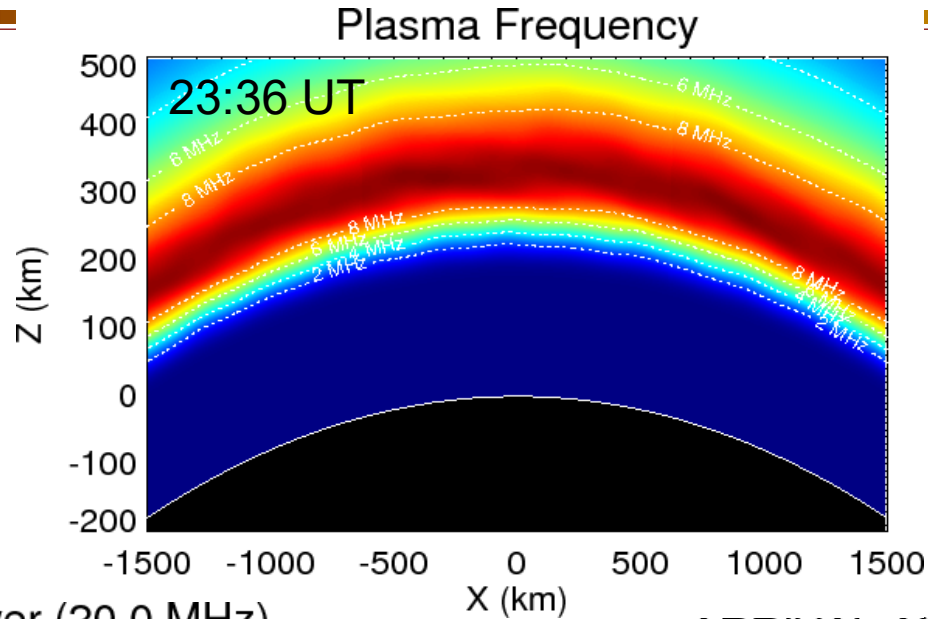


- Next few slides show PWE and ray-trace propagation through large scale plasma structures obtained via physics based simulation
- Measured neutral wind fields were used to initialize a physics based model (PBMOD), TIDs develop and seed R-T instability, producing spread-F plumes
- HF waves (20 MHz) were propagated through PBMOD data cubes in zonal direction at 4 time snapshots during the plasma evolution
- The propagation plots on slides 6-10 show
 - Plasma frequency (colors and contours)
 - Wave-optics (colors) and Ray-tracing (white curves) with plasma frequency contours
 - Spectrum of arrival angle at the ground (colors)

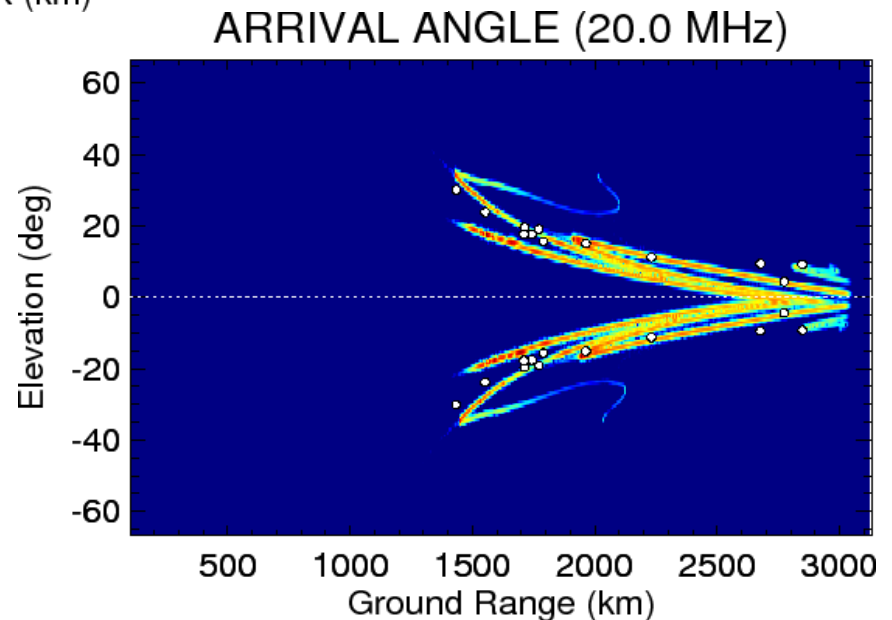
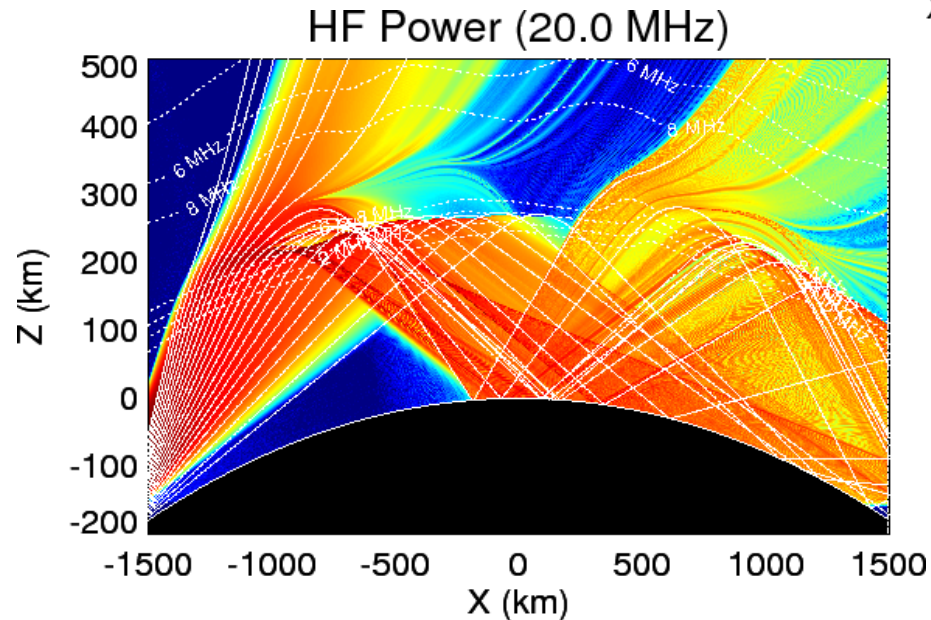
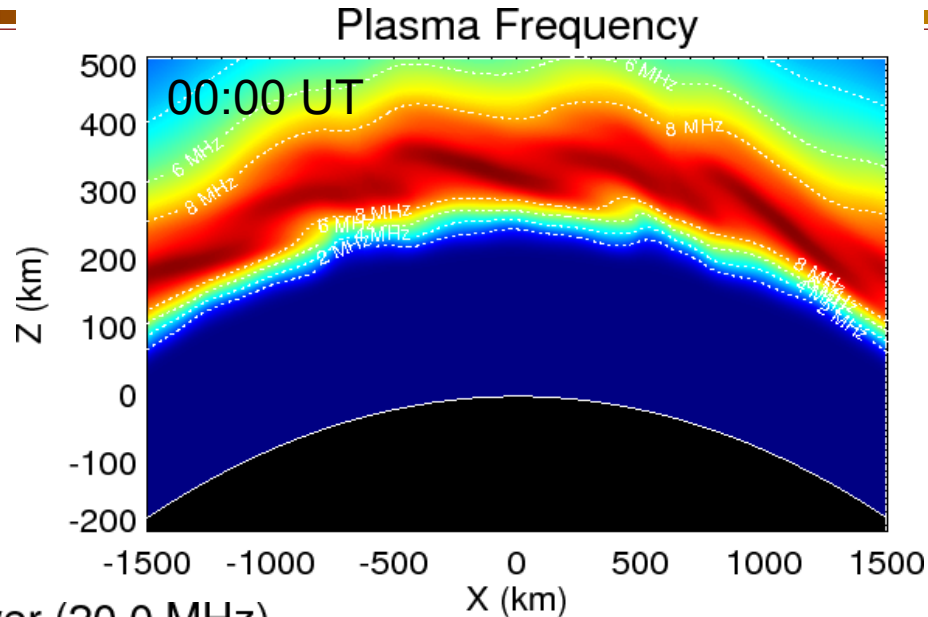
PBMOD simulations of the interchange instability in this event, showing plasma density in the equatorial plane. TIDDBIT data provided the neutral-wind perturbations.



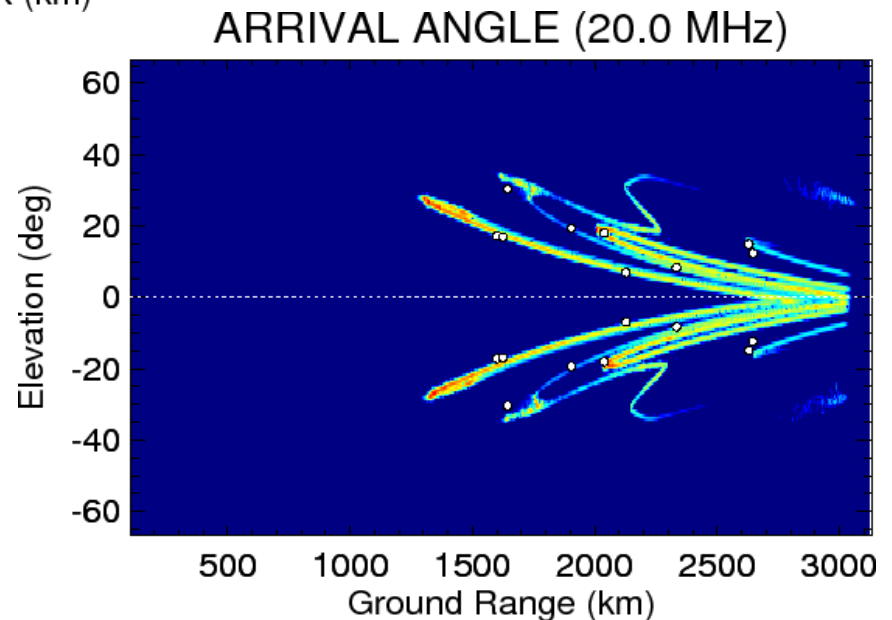
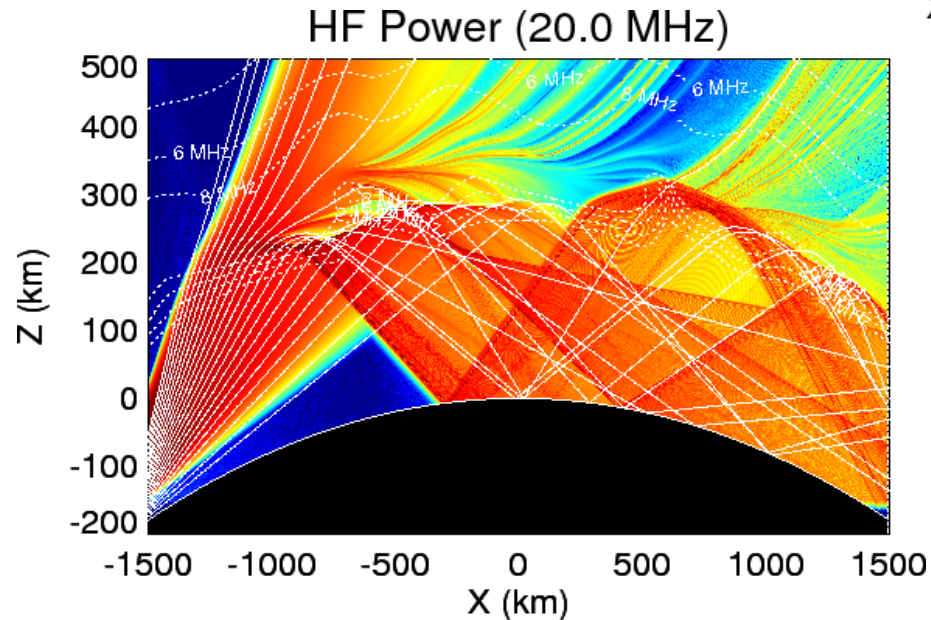
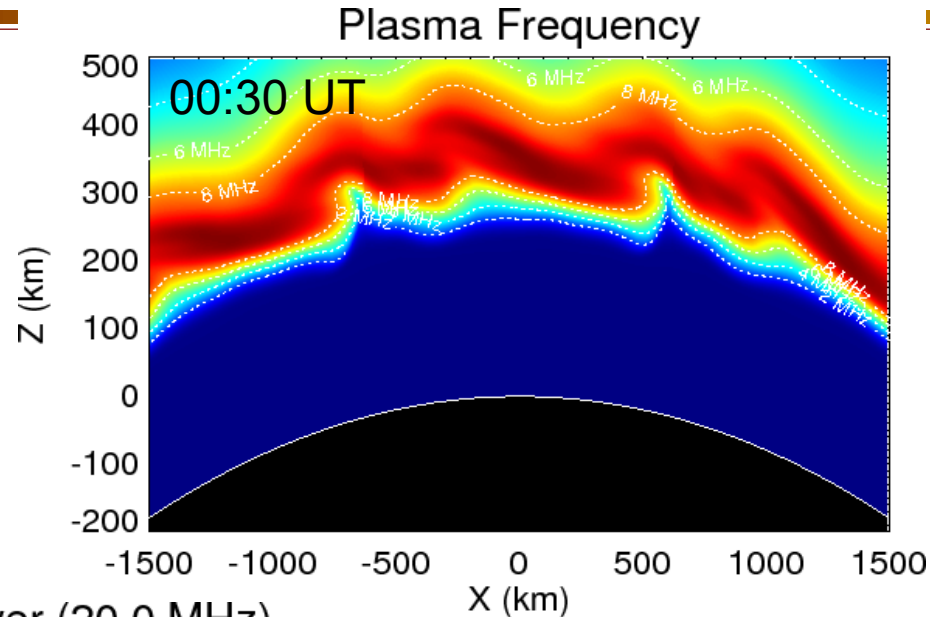
Propagation through Simulated TIDs



Propagation through Simulated TIDs



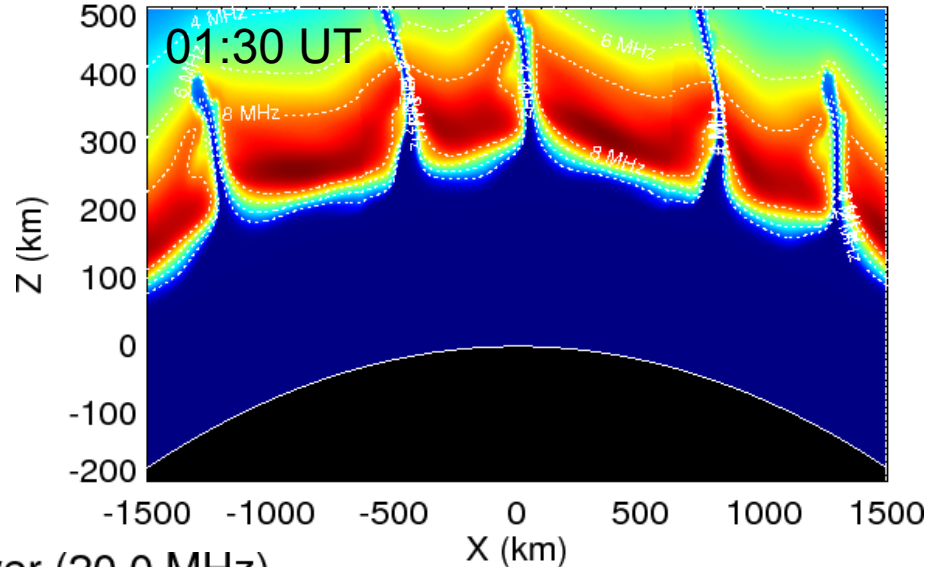
Propagation through Simulated TIDs



Propagation through Simulated TIDs

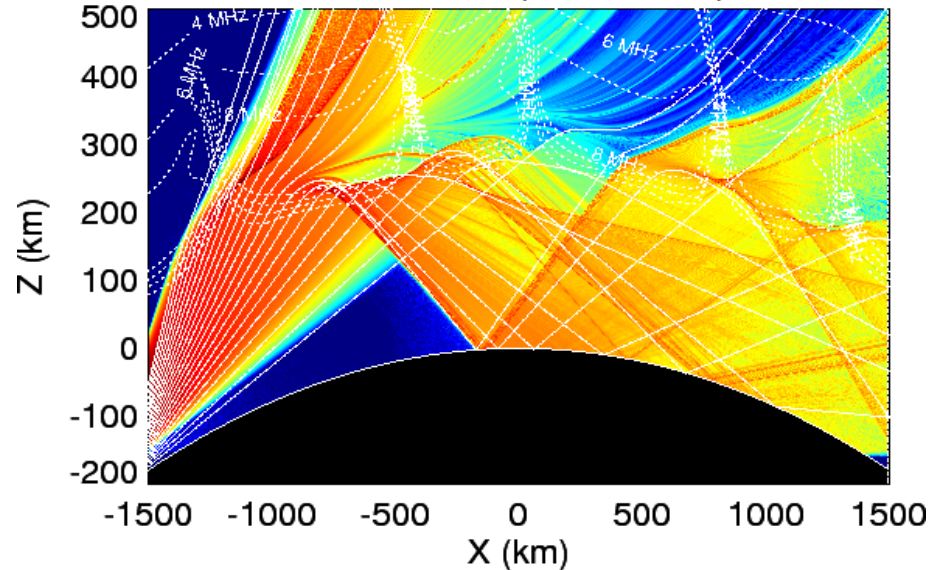


Plasma Frequency

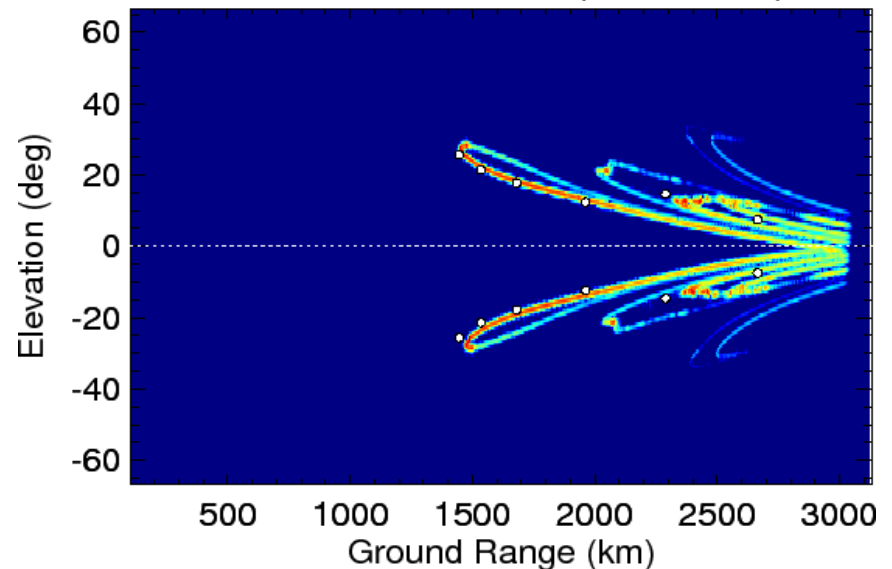


The number of propagation modes increases as the ionospheric structure develops. Ray-tracing results appear random, but wave-optics reveals systematic behavior of complex propagation environment

HF Power (20.0 MHz)



ARRIVAL ANGLE (20.0 MHz)



- Theory suggests wave-optics and ray-tracing should predict the same arrival angles when refractive processes are dominant e.g. when the scale sizes of the irregularities are much larger than the wavelength.
- Our PBMOD simulations support structure with scale-sizes of about 10 km. In the absence of sub-grid scale structure, we observed good agreement between wave-optics and ray-tracing, except in regions of strong focusing following caustics.
- Wave-optics provides more information than ray-tracing, as both the spectra of wave power and direction are available everywhere. This additional information is most useful when the propagation environment is multi-modal.
- Under these conditions, ray-tracing results become difficult to interpret because the footprints appear to be distributed randomly. The wave-optics results show that while the propagation environment is complex, it remains deterministic and systematic, with multiple modes of propagation clearly defined for all ranges.
- We believe the additional information afforded by wave-optics can be leveraged to improve OTHR performance.